

M1.

Full evaluation referencing that the steps are right but the order is wrong, giving the correct order

oe

B1 for a partial explanation eg references incorrect order without being specific

B2**[2]****M2.**

$$\frac{1}{125^{\frac{2}{3}}} \text{ or } 5^{-2} \text{ or } (\sqrt[3]{125})^{-2}$$

$$\text{or } \sqrt[3]{125} = 5$$

M1

$$\frac{1}{(\sqrt[3]{125})^2} \text{ or } \frac{1}{(\sqrt[3]{125})^2} \text{ or } \left(\frac{1}{(\sqrt[3]{125})^2}\right)^2$$

$$\text{or } \sqrt[3]{\left(\frac{1}{125}\right)^2} \text{ or } 125^{\frac{2}{3}} = 25$$

$$\text{or } \frac{1}{5^2} \text{ or } \left(\frac{1}{5}\right)^2 \text{ or } 25^{-1} \text{ or } 0.2^2$$

M1dep

$$\frac{1}{25}$$

oe 0.04

A1**[3]**

M3.101. $4^{\frac{1}{2}}$ estimated as 10

condone - 10

B1

$$(6.43^0 =) 1$$

B1

$$7.99^{\frac{2}{3}} \text{ estimated as } 4$$

B1

14

condone -6 if -10 used
ft fully correct evaluation with B2 scored

B1ft

[4]

M4.

(a) x^7

$$\text{B1 } \sqrt{x^{14}} \text{ or } (x^{14})^{\frac{1}{2}} \text{ or } \sqrt{x^{5-9}}$$

$$\text{or } (x^{5-9})^{\frac{1}{2}} \text{ or } x^{\frac{14}{2}} \text{ or } x^{\frac{5-9}{2}}$$

$$\text{or } x^{\frac{5}{2}} \times x^{\frac{9}{2}} \text{ or } x^{2.5} \times x^{4.5}$$

B2

(b) 0.2 or $\frac{1}{5}$ or 5^{-1}

$$\text{B1 } 125^{-\frac{1}{3}} \text{ or } \sqrt[3]{125}$$

$$\text{or } \left(\frac{1}{125}\right)^{\frac{1}{3}} \text{ or } \sqrt[3]{\frac{1}{125}}$$

$$\text{or } \frac{1}{125^{\frac{1}{3}}} \text{ or } \frac{1}{\sqrt[3]{125}}$$

$$\text{or } \left(\frac{1}{5^3}\right)^{\frac{1}{3}} \text{ or } \sqrt[3]{\frac{1}{5^3}}$$

$$\text{or } \frac{1^{\frac{1}{3}}}{5} \text{ or } \frac{\sqrt[3]{1}}{5}$$

$$\text{or } \frac{1}{y^3} = 125 \quad \text{or } y^3 = \frac{1}{125} \quad \text{or } \frac{1}{y} = 5$$

$$\text{or } \frac{1}{y} = \sqrt[3]{125} \quad \text{or } \frac{1}{y} = 125^{\frac{1}{3}}$$

B2

[4]

$$\text{M5. } 8^{\frac{1}{3}} \quad \text{or } \frac{1}{\sqrt[3]{8^2}} \quad \text{or } \frac{1}{(\sqrt[3]{8})^2} \quad \text{or } \sqrt[3]{8} = 2$$

$$\text{or } \frac{1}{2^2} \quad \text{or } 2^{-2} \quad \text{or } 4^{-1} \quad \text{or } 2^2 = 4$$

M1

$$\frac{1}{4} \quad \text{or } 0.25$$

A1

[2]

$$\text{M6. } m = 5$$

B1

$$(3^2)^p = 3^m \quad \text{or } 3^{2p} = 3^m$$

$$\text{or } (3^2)^p = 3^{\text{their } 5} \quad \text{or } 3^{2p} = 3^{\text{their } 5}$$

$$\text{or } 3^5 = 243 \quad \text{or } 3^{\text{their } 5} = (\sqrt{9})^{\text{their } 5}$$

or $3^{\text{their } 5}$ correctly evaluated

$$9^p = 9^{\frac{m}{2}} \quad \text{or } 9^p = 3^{\text{their } 5}$$

$$\text{or } 9^p = 243 \quad \text{or } 3^{2p} = 243$$

oe

M1

$$2p = m \text{ or } 2p = \text{their } 5 \text{ or } 9^p = 9^{\frac{\text{their } 5}{2}}$$

oe

M1

$$p = 2.5$$

oe

ft for values of m and p where $p = \frac{m}{2}$

A1ft

[4]

M7.

$$x^{-\frac{2}{3}} \text{ or } a = -\frac{2}{3}$$

B2 $(x^{\frac{-1}{3}})^2$ or $(x^2)^{\frac{-1}{3}}$ or $(x^{\frac{2}{3}})^{-1}$ or
 $(x^{-2})^{\frac{1}{3}}$ or $(x^{\frac{1}{3}})^{-2}$ or $\frac{1}{x^{\frac{2}{3}}}$ or $-\frac{2}{3}$

B1 $(\sqrt[3]{x})^2$ or $(\sqrt[3]{x^2})^{-1}$ or $(\frac{1}{x^2})^{\frac{1}{3}}$
 or $\frac{1}{(x^2)^{\frac{1}{3}}}$ or $(\frac{1}{\sqrt[3]{x}})^2$

or base x with any negative index.

B3

[3]

M8. Correct evaluation of a relevant power of 2 or 16

eg $16^{\frac{1}{2}} = (\pm) 4$ or $16^{\circ} = 256$ or $2^4 = 16$ or

or $4^c = d$

$16^{\frac{1}{4}} = (\pm) 2$ or $16^i = 16$ or $16^o = 1$

M1

One correct pair of answers

A correct answer is such that $d = 4c$

A1

A second correct pair of answers

eg $c = 0, d = 0$

$c = 1, d = 4$ or $c = -1, d = -4$

$c = 2, d = 8$ or $c = \frac{1}{8}, d = \frac{1}{2}$ etc ...

A1
[3]

M9. $(\sqrt[3]{64})^2$ or $(\sqrt[3]{64^2})$ or 4^2 or $\sqrt[3]{4096}$

M1

16

A1

[2]

M10. (a) $\frac{1}{27}$

B2 for 27 or $\frac{1}{3}$ or $\frac{1}{729}$ or 27^{-1}

B1 for 3 or 729 or $\frac{1}{9^2}$ or -27

B3

(b) $2^{3m} (= 2^{m^2})$ or $(2^3)^m (= 2^{m^2})$

oe

M1

$m^2 = 3m$ or $m^2 - 3m = 0$ or $m(m - 3) = 0$

or $(m =) 0$ or $(m =) 3$

oe

M1 dep

0 and 3

A1

[6]

M11. $\sqrt[3]{27} (= 3)$ or 27^2 or 729
Do not allow $\sqrt[3]{27} = 9$

M1

9

A1

[2]

M12. (a) Sight of $\sqrt{4} = 2$ followed by 2^3 or 4^3 followed by $\sqrt{64}$
B1 for partial solution but incomplete
eg for $\sqrt{4} = 2$ seen or 64 seen

B2

(b) $(4^y) = (4^{1.5})^6$ or $(2^y) = (2^3)^6$
Allow 1.5×6 or $2 \times y = 3 \times 6$

M1

9

Allow $\frac{18}{2}$ and 4^9

A1

[4]

M13.B1 for $64^{\frac{1}{3}} = 4$

B1 for $4^{\frac{3}{2}} = 8$

B1 for $27^{\frac{2}{3}} = 9$

B3
[3]

M14.

$$\frac{4}{3}\pi x^3 (=) \frac{2}{3}\pi y^3$$

oe e.g. 1 $\frac{4}{3}\pi \times x^3 (=) \frac{1}{2} \times \frac{4}{3}\pi \times y^3$
e.g. 2 $y^3 = 2x^3$

M1

$$\left(\frac{y^3}{x^3} =\right) \frac{\frac{4}{3}\pi}{\frac{2}{3}\pi} \text{ or } y = \sqrt[3]{2}x$$

oe e.g. $\frac{y^3}{x^3} = 2$

M1dep

$$2^{\frac{1}{3}}$$

$\sqrt[3]{2}$ scores M2 A0

A1

[3]

M15. $9^{\frac{1}{2}} = 3$ or $(-7)^{\circ} = 1$

B1

$$\left(\frac{1}{8}\right)^{-\frac{1}{3}} = 8^{\frac{1}{3}} \quad \text{or} \quad \frac{1}{\sqrt[3]{\frac{1}{8}}} \quad \text{or} \quad \frac{1}{\frac{1}{2}} \quad \text{or} \quad \sqrt[3]{8} \quad \text{or} \quad \frac{1}{\frac{1}{2}} \quad \text{implies M1}$$

$$\text{or} \quad \left(\frac{1}{2}\right)^{-1} \quad \text{or} \quad \left(\frac{1}{8}\right)^{\frac{1}{3}} = \frac{1}{2} \quad \text{or} \quad \sqrt[3]{8} = \frac{1}{2}$$

M1

$$\left(\frac{1}{8}\right)^{-\frac{1}{3}} = 2$$

A1

All three numbers correctly evaluated and in correct order

$$(-7)^{\circ}$$

$$\left(\frac{1}{8}\right)^{-\frac{1}{3}}$$

$$9^{\frac{1}{2}}$$

A1

[4]